

Game Theory, PhD in Economics and Management, 2005/06  
Exercises, sheet no. 1, Monday, November 7, 2005

**Exercise 1** Let  $u : \mathbb{R} \rightarrow \mathbb{R}$  be a von Neumann - Morgenstern utility function. Find a couple of lotteries which are evaluated in an opposite way by  $u$  and by  $v = u^3$

**Exercise 2** Give an appropriate definition for a symmetric game (in strategic form, two players).

Discuss the properties of dominant (strong, strict, weak) and dominated strategies, iteratively undominated strategies and Nash equilibria.

**Exercise 3** If we delete strongly dominated strategies, what happens to the Nash equilibria of a strategic game (with  $n$  players)? Same question for strict and weak dominance

**Exercise 4** Consider the following game. There are  $n$  players. Each one has to name a number in  $\{1, \dots, 100\}$ . Whoever gets closest to the  $2/3$  of the mean of the number that were named, wins.

Add the details needed to have a game in strategic form and find its pure Nash equilibria (if any).

**Exercise 5** Describe (draw? paint?) a game in extensive form, with at least one chance move and one non trivial information set. Describe its strategic form.